



Frontiers of Graph Neural Networks with DIG

https://github.com/divelab/DIG/

Shuiwang Ji, Yaochen Xie, Zhao Xu, Haiyang Yu

Schedule



Graph neural networks	20 min	Shuiwang Ji
Self-supervised learning	35 min	Yaochen Xie
Practical session: dig.sslgraph	15 min	Zhao Xu
Q&A	10 min	All
Explainability	35 min	Haiyang Yu
Practical session: dig.xgraph	15 min	Haiyang Yu
Q&A	10 min	All

Success of Deep Learning

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Deep learning shines on many tasks



Image Classification



Machine Translation



Speech recognition

Graphs



Objects + Relationships = Graph





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Tasks over Graphs



- Node-level classification/regression
- Graph-level classification/regression
- Link prediction
- Generation
- Explainability
-



Tasks on Graph Data



- e.g., Node classification
 - Document classification in a citation network



Tasks on Graph Data



- e.g., Graph classification
 - Molecular property prediction



Tasks on Graph Data



- e.g., Link prediction
 - Friend suggestion in a social network





Graph Neural Networks: Basic Concepts

https://github.com/divelab/DIG/

Notations

- G = (X, A)
- Adjacency matrix
- $A:\begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix} \in R^{N \times N}$ Feature matrix

$$X:\begin{bmatrix} 9 & 2\\ 5 & 3\\ 4 & 4\\ 1 & 6 \end{bmatrix} \in R^{N \times d}$$



• We will consider edge features later



Permutation



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$$X:\begin{bmatrix} 9 & 2\\ 5 & 3\\ 4 & 4\\ 1 & 6 \end{bmatrix} \in R^{N \times d} \qquad A:\begin{bmatrix} 0 & 1 & 1 & 1\\ 1 & 0 & 0 & 0\\ 1 & 0 & 0 & 1\\ 1 & 0 & 1 & 0 \end{bmatrix} \in R^{N \times N}$$



Permutation

$$X: \begin{bmatrix} 9 & 2 \\ 5 & 3 \\ 4 & 4 \\ 1 & 6 \end{bmatrix} \in \mathbb{R}^{N \times d} \qquad A: \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix} \in \mathbb{R}^{N \times N}$$

$$X': \begin{bmatrix} 5 & 3\\ 1 & 6\\ 9 & 2\\ 4 & 4 \end{bmatrix} \in R^{N \times d} \qquad A': \begin{bmatrix} 0 & 0 & 1 & 0\\ 0 & 0 & 1 & 1\\ 1 & 1 & 0 & 1\\ 0 & 1 & 1 & 0 \end{bmatrix} \in R^{N \times N}$$



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Permutation



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$$X: \begin{bmatrix} 9 & 2\\ 5 & 3\\ 4 & 4\\ 1 & 6 \end{bmatrix} \in \mathbb{R}^{N \times d} \qquad A: \begin{bmatrix} 0 & 1 & 1 & 1\\ 1 & 0 & 0 & 0\\ 1 & 0 & 1 & 0 \end{bmatrix} \in \mathbb{R}^{N \times N}$$

$$X' = PX; A' = PAP^{T} \qquad P: \begin{bmatrix} 0 & 1 & 0 & 0\\ 0 & 1 & 0 & 0\\ 0 & 0 & 0 & 1\\ 1 & 0 & 0 & 0\\ 0 & 0 & 1 & 0 \end{bmatrix} \in \{0,1\}^{N \times N}$$

$$X': \begin{bmatrix} 5 & 3\\ 1 & 6\\ 9 & 2\\ 4 & 4 \end{bmatrix} \in \mathbb{R}^{N \times d} \qquad A': \begin{bmatrix} 0 & 0 & 1 & 0\\ 0 & 0 & 1 & 1\\ 1 & 1 & 0 & 1\\ 0 & 1 & 1 & 0 \end{bmatrix} \in \mathbb{R}^{N \times N}$$





Permutation Invariance



- For graph-level representations
 - We learn a function f that maps a graph G = (X, A) to a representation vector $\in \mathbb{R}^{d'}$

 $f(X,A) = f(PX, PAP^T)$

- P is any permutation matrix



Permutation Equivariance



- For node-level representations
 - We learn a function *f* that maps a graph G = (X, A) to a node representation matrix $\in \mathbb{R}^{N \times d'}$

 $Pf(X,A) = f(PX,PAP^T)$





Graph Neural Networks

Partially based on materials at: https://geometricdeeplearning.com/lectures/

Overview



 GNNs are composed of multiple permutation equivariant/invariant layers/functions



Michael M. Bronstein, Joan Bruna, Taco Cohen, Petar Veličković, Geometric Deep Learning: Grids, Groups, Graphs, Geodesics, and Gauges.

Idea



Neighborhood aggregation!

- Neighborhood features $X_{\mathcal{N}_i} = \{\{x_j : j \in \mathcal{N}_i\}\}$
- Define a local function $\phi(x_i, X_{\mathcal{N}_i})$

$$H = f(X, A) = \begin{bmatrix} \phi(x_1, X_{\mathcal{N}_1}) \\ \dots \\ \phi(x_N, X_{\mathcal{N}_N}) \end{bmatrix}$$



Michael M. Bronstein, Joan Bruna, Taco Cohen, Petar Veličković, Geometric Deep Learning: Grids, Groups, Graphs, Geodesics, and Gauges.





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What's in a GNN layer



- We build permutation equivariant functions f(X, A)on graphs by sharing the local permutation invariant function $\phi(x_i, X_{\mathcal{N}_i})$
- How to implement ϕ ?

 $H = f(X, A) = \begin{bmatrix} \phi(x_1, X_{\mathcal{N}_1}) \\ \dots \\ \phi(x_N, X_{\mathcal{N}_N}) \end{bmatrix}$



Michael M. Bronstein, Joan Bruna, Taco Cohen, Petar Veličković, Geometric Deep Learning: Grids, Groups, Graphs, Geodesics, and Gauges.

Three "flavours" of GNN layers



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Frontier Topics of GNN



- Self-supervised learning of GNNs
 - Studies how to train GNNs with unlabeled graph data
 - Applications: pre-training in drug discovery, node representation learning for industrial large-scale graphs.
- GNN explainability
 - Studies the cause of GNN predictions
 - Applications: building trustworthy and transparent GNN models
- Graph generation, 3D geometric GNNs, etc.



Self-Supervised Learning on Graphs

https://github.com/divelab/DIG/



Self-supervised Learning

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- Training models with self-supervision.
- Success in text and image data. We see an explosion of graph SSL papers.
- Three paradigms of using self-supervised learning
 - Unsupervised representation learning
 - Unsupervised pre-training
 - Auxiliary learning





Xie et al. Self-Supervised Learning of Graph Neural Networks: A Unified Review. TPAMI, 2022.

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Taxonomy of SSL Methods

Contrastive vs Predictive: are negative pairs required?

- Contrastive
 - Maximizes mutual information
 - Focuses on designing view generation
- Predictive
 - Ad-hoc pretext-tasks / information bottleneck
 - Focuses on designing task/objective

Xie et al. Self-Supervised Learning of Graph Neural Networks: A Unified Review. TPAMI, 2022.



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Taxonomy of SSL Methods



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Xie et al. Self-Supervised Learning of Graph Neural Networks: A Unified Review. TPAMI, 2022.

Contrastive Methods



- Representations of "similar" graph data to be closer, and that of "dissimilar" graph data to be further from each other.
- In practice, we do not have ground-truth or defined measurement for similarity. We construct augmented graphs (or subgraphs) from the same graph to be "similar", and different graph samples are "dissimilar".

Contrastive Methods



- Representations of "similar" graph data to be closer, and that of "dissimilar" graph data to be further from each other.
- Theoretical grounding: mutual information maximization. Jointly sampled graphs are "similar", while independently sampled graphs are "dissimilar"

$$\mathcal{I}(\boldsymbol{x}, \boldsymbol{y}) = D_{KL}(p(\boldsymbol{x}, \boldsymbol{y}) || p(\boldsymbol{x}) p(\boldsymbol{y}))$$

- We consider a graph as a random variable and obtain two views of the graph.
- Representations of the two views are x and y. A good GNN should encode two views into representation that share as much mutual information as possible.

Contrastive Methods



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Xie et al. Self-Supervised Learning of Graph Neural Networks: A Unified Review. TPAMI, 2022.

Contrastive Objectives



- Derived as lower bounds of mutual information
 - Jensen-Shannon Estimator (DGI, InfoGraph, MVGRL, etc.)

$$\begin{aligned} \widehat{\mathcal{I}}^{(JS)}(\boldsymbol{h}_{i},\boldsymbol{h}_{j}) &= \mathbb{E}_{(\boldsymbol{A},\boldsymbol{X})\sim\mathcal{P}}\left[\log(\mathcal{D}(\boldsymbol{h}_{i},\boldsymbol{h}_{j}))\right] + \\ & \mathbb{E}_{\left[(\boldsymbol{A},\boldsymbol{X}),(\boldsymbol{A}',\boldsymbol{X}')\right]\sim\mathcal{P}\times\mathcal{P}}\left[\log(1-\mathcal{D}(\boldsymbol{h}_{i},\boldsymbol{h}'_{j}))\right] \end{aligned}$$

• InfoNCE (GraphCL, GRACE, etc.)

$$\begin{aligned} \widehat{\mathcal{I}}^{(\text{NCE})}(\boldsymbol{h}_{i},\boldsymbol{h}_{j}) &= \mathbb{E}_{(\boldsymbol{A},\boldsymbol{X})\sim\mathcal{P}} \left[\mathcal{D}(\boldsymbol{h}_{i},\boldsymbol{h}_{j}) - \mathbb{E}_{\boldsymbol{K}\sim\mathcal{P}^{N}} \left[\log \sum_{(\boldsymbol{A}',\boldsymbol{X}')\in\boldsymbol{K}} e^{\mathcal{D}(\boldsymbol{h}_{i},\boldsymbol{h}_{j}')} / N \middle| (\boldsymbol{A},\boldsymbol{X}) \right] \right] \\ &= \mathbb{E}_{[(\boldsymbol{A},\boldsymbol{X}),\boldsymbol{K}]\sim\mathcal{P}\times\mathcal{P}^{N}} \left[\log \frac{e^{\mathcal{D}(\boldsymbol{h}_{i},\boldsymbol{h}_{j})}}{\sum_{(\boldsymbol{A}',\boldsymbol{X}')\in\boldsymbol{K}} e^{\mathcal{D}(\boldsymbol{h}_{i},\boldsymbol{h}_{j}')}} \right] + \log N \end{aligned}$$

Xie et al. Self-Supervised Learning of Graph Neural Networks: A Unified Review. TPAMI, 2022.

View generation



• Three types of graph transformations for view generation



Xie et al. Self-Supervised Learning of Graph Neural Networks: A Unified Review. TPAMI, 2022.

What are good views for graphs?

• Ideally, good views (v_1 , v_2) generated for contrastive learning should

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- Have their mutual information $I(v_1, v_2)$ minimized
- Subject to $I(v_1, y) = I(v_2, y) = I(x, y)$



• The principle is even more important for graphs.

Tian et al. What Makes for Good Views for Contrastive Learning? NeurIPS 2020

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• BGRL



Thakoor et al., Large-Scale Representation Learning on Graphs via Bootstrapping. ICLR 2022.

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• CCA-SSG



Zhang et al., From Canonical Correlation Analysis to Self-supervised Graph Neural Networks. NeurIPS 2021.

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• LaGraph



Xie et al., Self-Supervised Representation Learning via Latent Graph Prediction. ICML 2022.

• Similarity

- Do not requires negative samples.
- Better scalability.
- Their objectives include a term to regularize the invariance of representations to different views (minimize their distance)

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• Effectiveness can be justified by the Information Bottleneck Principle

• Difference

- The formulation of entire objectives are different.
- Based on or derived from different theoretical grounding/insights
- Different technique to guarantee informative representations





DIG.sslgraph





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Next session: Explainability of GNNs



Explainability of GNNs

https://github.com/divelab/DIG/



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Why Explainability

Good performance but

- People don't understand deep model
 - taking it as black box

- People don't trust deep model
 - when the model fails



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Explainability:

Provide human-intelligible explanations to build trustworthy AI

Reference: https://towardsdatascience.com/guide-to-interpretable-machine-learning-d40e8a64b6cf



Challenges



- How to explain GNNs with edge information
 - Instance-level: edge-based, subgraph-based
 - Model-level: xgnn
- How to get human-understandable explanation results
 - Graph Sentiment dataset



- How to compare explainability methods systematically
 - Quantitative metrics: Fidelity+, Fidelity-, Sparsity

Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey. TPAMI 2022.

Overview of methods





Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey. TPAMI, 2022

Explanation on GNNs



Assigning importance scores on edges



Assigning importance scores on connected subgraphs



GNNExplainer

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A: Edge masks for class-distinguish important edges B: Node masks for important node feature dimension.



Ying et al. GNNExplainer: Generating Explanations for Graph Neural Networks. NeurIPS, 2019.

GNNExplainer



Explanation based on edges

$$\min_M - \sum_{c=1}^C \mathbf{1}[y=c] \log P_\Phi(Y=y \mid G = A_c \odot \sigma(M_E), X = X_c \odot \sigma(M_X))$$

- It learns soft masks on graph edges and node features.
- The masks are randomly initialized and updated to maximum the mutual information between the original predictions and the perturbed graphs.

SubgraphX



Explanation based on subgraphs

$$\mathcal{G}^* = \operatorname*{argmax}_{|\mathcal{G}_i| \leq N_{\min}} \operatorname{Score}(f(\cdot), \mathcal{G}, \mathcal{G}_i)$$

• Explore the important subgraphs with Monte Carlo tree search algorithm

$$a^* = \operatorname*{argmax}_{a_j} Q(\mathcal{N}_i, a_j) + U(\mathcal{N}_i, a_j)$$

• Take Shapley value as the subgraph importance scores

$$arphi_i(v) = \sum_{S\subseteq N\setminus\{i\}} rac{|S|!\;(n-|S|-1)!}{n!} (v(S\cup\{i\})-v(S))$$

Yuan et al. On Explainability of Graph Neural Networks via Subgraph Explorations. ICML 2021.





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Yuan et al. On Explainability of Graph Neural Networks via Subgraph Explorations. ICML 2021.

Sentiment Graph Dataset



- Better human evaluations for the explainability results
 - Graph-SST2, Graph-SST5, Graph-Twitter



"lathan and diggs have considerable personal charm, and their screen rapport makes the old story new."

Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey. TPAMI 2022. *Yuan et al.* On Explainability of Graph Neural Networks via Subgraph Explorations. ICML 2021.

Evaluation Metrics



- Compare different explainability methods systematically
 - Fidelity+, Fidelity-, Sparisty

Benchmark of explainability methods using Fidelity and Sparsity





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Q&A



Thank you!

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xgraph benchmark



